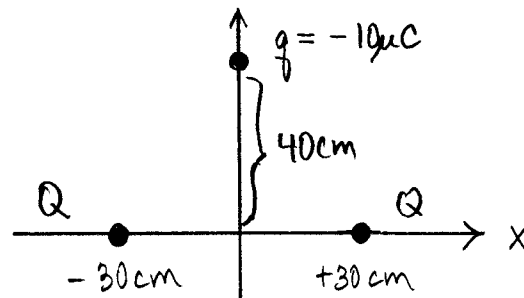


NAME: _____

SECTION #: _____

TA: _____

Two identical charges, Q , are placed on the x axis, one at $x = 30$ cm and the other at $x = -30$ cm. In an experiment you find that a 100 gram ball with charge $q = -10\mu\text{C}$ can be suspended (in equilibrium) 40 cm above the origin.



(a) Are the charges Q positive or negative?

Like charges repel, so Q must be negative

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$\vec{F} = q\vec{E}$$

$$k_e = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$$

$$g = 9.8 \text{ m/s}^2$$

(b) The charges Q produce an electric field at q . What is the direction of that field?

The force on q is upward, and since q is negative \vec{E} must be downward ($\vec{F} = q\vec{E}$ means \vec{E} + \vec{F} opposite for negative q)
 Alternatively, note that since Q is negative, the fields must point inward towards Q .

(c) Find the magnitude of that same electric field.

$$qE = mg \text{ so}$$

$$E = mg/q = (0.1\text{kg})(9.8\text{m/s}^2) / (10\mu\text{C})$$

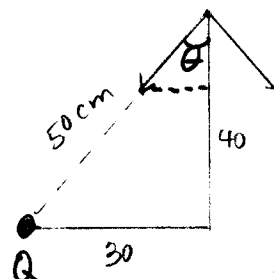
$E = 9.8 \times 10^4 \text{ N/C}$

(d) Find Q . From Coulomb's law the magnitude of the field is

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \text{ where } r = 0.5\text{m}$$

The x -components cancel and the y components add so

$$E_y = \left(\frac{1}{4\pi\epsilon_0}\right) \cdot 2 \cdot \frac{Q}{r^2} \cos\theta$$



$$\cos\theta = \frac{40}{50} = 0.8$$

$$Q = E_y \cdot r^2 / 2 \left(\frac{1}{4\pi\epsilon_0}\right) \cos\theta = 9.8 \times 10^4 \frac{\text{N}}{\text{C}} (0.5\text{m})^2 / 2 (9 \times 10^9) (0.8) = \boxed{1.7 \times 10^{-6} \text{ C}}$$