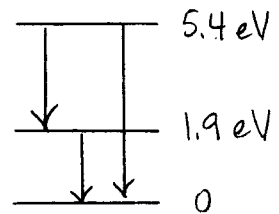


- 1) The drawing at the right shows the energy levels of a hypothetical atom. List the wavelengths (in nm) of all the lines that will be seen in the line spectrum of this atom.



$$E = hf = hc/\lambda \quad \lambda = \frac{hc}{E}$$

There are 3 possible lines, with energies 1.9 eV, 3.5 eV and 5.4 eV

$$\lambda_1 = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(3 \times 10^8 \text{ m/s})}{(1.9 \text{ eV})(1.602 \times 10^{-19} \text{ J/eV})} = 6.53 \times 10^{-7} \text{ m} = 653 \text{ nm}$$

$$\lambda_2 = \frac{(\text{ " }) (\text{ " })}{(3.5 \text{ eV}) (\text{ " })} = 354 \text{ nm}$$

$$\lambda_3 = \frac{(\text{ " }) (\text{ " })}{(5.4 \text{ eV}) (\text{ " })} = 230 \text{ nm}$$

653 nm, 354 nm, 230 nm

- 2) Ne has 10 electrons. List the quantum numbers n , l , m_l , m_s of each of the 10 electrons for Ne atoms in the ground state.

n	l	m_l	m_s
1	0	0	$+\frac{1}{2}$
1	0	0	$-\frac{1}{2}$
2	0	0	$+\frac{1}{2}$
2	0	0	$-\frac{1}{2}$
2	1	1	$+\frac{1}{2}$
2	1	1	$-\frac{1}{2}$
2	1	0	$+\frac{1}{2}$
2	1	0	$-\frac{1}{2}$
2	1	-1	$+\frac{1}{2}$
2	1	-1	$-\frac{1}{2}$

3) The nucleus ^{110}Ag has a half-life of 2.4 minutes.

$$2.4 \text{ min} = 144 \text{ s}$$

(a) Find the activity (decays per second) of a source consisting of 3×10^{10} atoms of ^{110}Ag .

$$\lambda = \frac{\ln 2}{T_{1/2}} = \frac{0.693}{144 \text{ s}} = 4.81 \times 10^{-3} / \text{s}$$

$$A = \lambda N = (4.8 \times 10^{-3} / \text{s})(3 \times 10^{10}) = 1.44 \times 10^8 / \text{s}$$

$$\boxed{1.44 \times 10^8 / \text{s}}$$

(b) What will the activity of the source be after 6 minutes have gone by? $6 \text{ min} = 360 \text{ s}$

$$N = N_0 e^{-\lambda t} = (3 \times 10^{10}) e^{-(4.81 \times 10^{-3})(360)} = 5.3 \times 10^9$$

$$A = \lambda N = 2.55 \times 10^7 / \text{s}$$

$$\boxed{2.55 \times 10^7 / \text{s}}$$

4) Find the deBroglie wavelength of an electron with a kinetic energy of 20 eV. The electron mass is $9.11 \times 10^{-31} \text{ kg}$.

$$KE = \frac{1}{2} m v^2 = \frac{(m v)^2}{2 m} = \frac{p^2}{2 m}$$

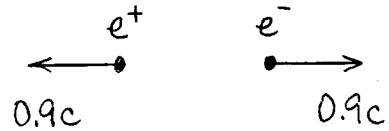
$$p = [2 m \cdot KE]^{1/2} = [2 (9.11 \times 10^{-31} \text{ kg}) \cdot (20 \text{ eV}) (1.602 \times 10^{-19} \text{ J/eV})]^{1/2}$$

$$p = 2.42 \times 10^{-24} \text{ kg} \cdot \text{m/s}$$

$$\lambda = h/p = \frac{6.626 \times 10^{-34} \text{ J} \cdot \text{s}}{2.42 \times 10^{-24} \text{ kg} \cdot \text{m/s}} = 2.74 \times 10^{-10} \text{ m}$$

$$\boxed{274 \text{ nm}}$$

- 5) An unstable particle, x , at rest in the lab decays spontaneously into an electron and a positron (both of which have rest mass 9.11×10^{-31} kg). In the decay the electron and the positron are emitted in opposite directions, each with speed $0.9c$.



- (a) What was the mass of particle x ?

Total energy is conserved $E_i = E_f$

$$E_i = m_x c^2$$

$$E_f = E_{e^+} + E_{e^-}$$

$$E_{e^-} = E_0 + KE = m_0 c^2 + (\gamma - 1)m_0 c^2 = \gamma m_0 c^2$$

$$\gamma = \left[\frac{1}{1 - v^2/c^2} \right]^{\frac{1}{2}} = \left(\frac{1}{1 - .81} \right)^{\frac{1}{2}} = 2.29$$

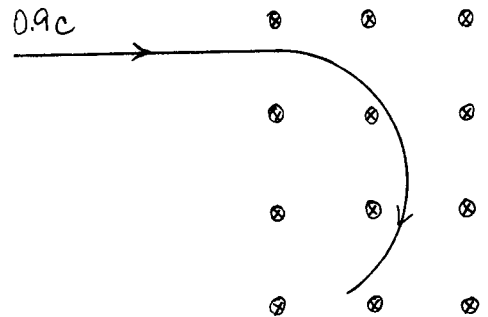
$$E_{e^-} = E_{e^+} = (2.29) m_0 c^2$$

So $m_x c^2 = 2 \times (2.29) m_0 c^2$

$$m_x = (2.29) \times (2) \times (9.11 \times 10^{-31} \text{ kg})$$

$$4.17 \times 10^{-30} \text{ kg}$$

- (b) Suppose the electron enters a region in which there is a uniform magnetic field of 0.8 T (into the page in the drawing). As it moves through the field the electron will follow a circular path. Find the radius of the circle.



$$R = \frac{mv}{qB}$$

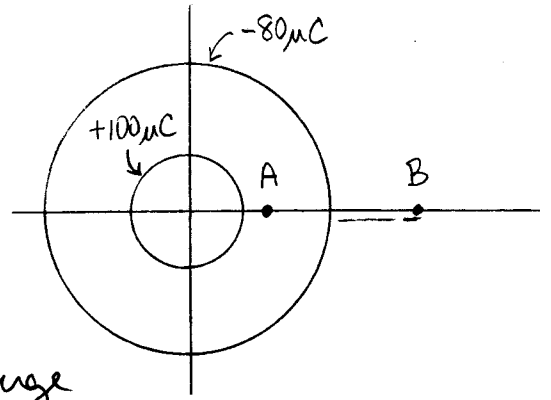
But we need to use the relativistic mass of the electron $m = \gamma m_0$

$$R = \frac{(2.29)(9.11 \times 10^{-31} \text{ kg})(0.9)(2.998 \times 10^8 \text{ m/s})}{(1.602 \times 10^{-19} \text{ C})(0.8 \text{ T})}$$

$$= 4.39 \times 10^{-3} \text{ m}$$

$$4.39 \text{ mm}$$

- 6) Two concentric hollow metal spheres have radii of 20 cm and 50 cm respectively. A charge of $+100\mu\text{C}$ is placed on the smaller sphere, and a charge of $-80\mu\text{C}$ is placed on the larger one. Find the magnitude of the electric field at point A (30 cm from the center of the spheres) and at point B (80 cm from the center).



At A there is no field from the outer charge

$$E = \left(\frac{1}{4\pi\epsilon_0}\right) \frac{100 \times 10^{-6} \text{ C}}{(0.3 \text{ m})^2} = 9.99 \times 10^6 \text{ V/m}$$

At B we get fields from both spheres. The net charge is now $+20\mu\text{C}$

$$E = \left(\frac{1}{4\pi\epsilon_0}\right) \frac{20 \times 10^{-6} \text{ C}}{(0.8 \text{ m})^2} = 2.81 \times 10^5 \text{ V/m}$$

Point A: $9.99 \times 10^6 \text{ V/m}$

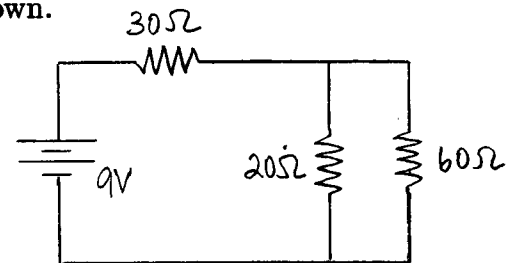
Point B: $2.81 \times 10^5 \text{ V/m}$

- 7) Find the total current supplied by the battery in the circuit shown.

$$\frac{1}{R_{||}} = \frac{1}{20\Omega} + \frac{1}{60\Omega} \Rightarrow R_{||} = 15\Omega$$

$$R_{\text{TOT}} = 30\Omega + 15\Omega = 45\Omega$$

$$I = \frac{V}{R} = \frac{9\text{V}}{45\Omega} = 0.2 \text{ A}$$



0.2 A