

NAME: SOLUTIONS

SECTION #: \_\_\_\_\_

TA: \_\_\_\_\_

A long straight wire carries a current of 20 A. A particle of mass  $m$  and charge  $q = 10 \mu\text{C}$  is 5 cm below the wire and traveling with a velocity of  $3 \times 10^4 \text{ m/s}$ .

(a) Find the magnitude and direction of the magnetic field that the particle feels.

Right hand rule with thumb along the wire  $\Rightarrow$  field lines loop around and at  $m$  point into the paper.

$$B = \frac{\mu_0 I}{2\pi r} = \frac{(4\pi \times 10^{-7} \text{ T}\cdot\text{m/A})(20 \text{ A})}{2\pi \cdot (0.05 \text{ m})} = \boxed{8.0 \times 10^{-5} \text{ T}}$$

$$\begin{aligned} \vec{F} &= q\vec{E} \\ F &= qvB \sin \theta \\ F &= IBL \sin \theta \\ B &= \frac{\mu_0 I}{2\pi r} \\ \mu_0 &= 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A} \end{aligned}$$

(b) Find the magnitude and direction of the force on the particle if it is moving in the  $+x$  direction.

Direction: fingers along  $v$ , curl to  $\vec{B}$  (into paper)  $\Rightarrow$  thumb points upward ( $+y$ )

$$F = qvB \sin \theta \quad \theta = 90^\circ, \sin \theta = 1$$

$$F = (10^{-5} \text{ C})(3 \times 10^4 \text{ m/s})(8 \times 10^{-5} \text{ T}) = \boxed{2.4 \times 10^{-5} \text{ N}}$$

(c) Find the magnitude and direction of the force on the particle if it is moving in the  $+y$  direction.

Direction: fingers along  $+y$ , curl into paper  $\Rightarrow$  force is to the left ( $-x$  direction)

$$F = qvB \sin \theta = \text{same as (b)} = \boxed{2.4 \times 10^{-5} \text{ N}}$$

(d) Find the magnitude and direction of the force on the particle if it is moving into the paper.

Here  $\vec{v}$  and  $\vec{B}$  are parallel,  $\theta = 0$ ,  $\sin \theta = 0$

$$\boxed{F = 0}$$