

Constants: $c = 2.998 \times 10^8 \text{ m/s}$ $e = 1.602 \times 10^{-19} \text{ C}$ $N_A = 6.02 \times 10^{23}$

$$k_B = 1.38 \times 10^{-23} \text{ J/K} \quad m_e = 511 \text{ keV}/c^2 \quad \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$$

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s} \quad \hbar = h/2\pi \quad 1 \text{ eV} = 1.602 \times 10^{-19} \text{ J} \quad R = 1.09737 \times 10^7/\text{m}$$

$$hc = 1240 \text{ eV}\cdot\text{nm} \quad \frac{e^2}{4\pi\epsilon_0} = 1.44 \text{ eV}\cdot\text{nm} \quad 1 \text{ u} = 931.5 \text{ MeV}/c^2 \quad a_0 = 0.0529 \text{ nm}$$

Classical Physics:

$$\vec{F} = m\vec{a} \quad K = \frac{1}{2}mv^2 \quad a = \frac{v^2}{r} \quad F_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r^2} \quad V_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r}$$

Modern Physics:

$$p = \frac{h}{\lambda} = \hbar k \quad E = hf = \hbar\omega \quad v_{\text{phase}} = \frac{\omega}{k} \quad v_{\text{group}} = \frac{d\omega}{dk} \quad a_0 = \frac{4\pi\epsilon_0 \hbar^2}{e^2 m}$$

$$\Delta p \Delta x \geq \frac{\hbar}{2} \quad \Delta E \Delta t \geq \frac{\hbar}{2} \quad \Delta x = [\langle x^2 \rangle - \langle x \rangle^2]^{1/2}$$

$$-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \Psi(x, t) + V(x)\Psi(x, t) = i\hbar \frac{\partial}{\partial t} \Psi(x, t) \quad P(x) = |\Psi(x, t)|^2 = \Psi^*(x, t) \Psi(x, t)$$

$$-\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi(x, t) + V(x)\psi(x, t) = E\psi(x, t) \quad \Psi(x, t) = \psi(x) e^{-iEt/\hbar} \quad \int_{-\infty}^{\infty} P(x) dx = 1$$

$$\langle x \rangle = \int_{-\infty}^{\infty} \psi^*(x) x \psi(x) dx \quad \langle f(x) \rangle = \int_{-\infty}^{\infty} \psi^*(x) f(x) \psi(x) dx \quad \langle p \rangle = \int_{-\infty}^{\infty} \psi^*(x) \frac{\hbar}{i} \frac{d}{dx} \psi(x) dx$$

$$\text{Square Well: } \psi_n = \sqrt{\frac{2}{L}} \sin \frac{n\pi}{L} x; \quad E_n = \frac{n^2 \pi^2 \hbar^2}{2mL^2} \quad \text{Oscillator: } E_n = (n + \frac{1}{2}) \hbar\omega$$

$$T = \left[1 + \frac{V_0^2}{16E(V_0 - E)} (e^{\alpha L} - e^{-\alpha L})^2 \right]^{-1} \quad T \simeq e^{-2G} \quad G = \sqrt{\frac{2m}{\hbar^2}} \int [V(x) - E]^{\frac{1}{2}} dx$$

$$\psi_{n,\ell,m} = R_{n,\ell}(r) Y_{\ell}^m(\theta, \phi) \quad E_n = -\frac{1}{2} \left(\frac{e^2}{4\pi\epsilon_0} \right)^2 \frac{m}{\hbar^2} \frac{1}{n^2} = -\frac{13.6 \text{ eV}}{n^2} \quad P(r) = r^2 R_{n,\ell}^2$$

$$\ell = 0, 1, 2, \dots, n-1 \quad m = -\ell, -\ell+1, \dots, \ell \quad L = \sqrt{\ell(\ell+1)} \hbar \quad L_z = m\hbar$$