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## EXAM 1

Print your name and section clearly on all five pages. (If you do not know your section number, write your TA's name.) Show all work in the space immediately below each problem. Your final answer must be placed in the box provided. Problems will be graded on reasoning and intermediate steps as well as on the final answer. Be sure to include units wherever necessary, and the direction of vectors. Each problem is worth 25 points. In doing the problems, try to be neat. Check your answers to see that they have the correct dimensions (units) and are the right order of magnitudes. You are allowed one 5 " $\times 8$ " note card and no other references. The exam lasts exactly one hour.
(Do not write below)

## SCORE:

Problem 1: $\qquad$

Problem 2: $\qquad$

Problem 3: $\qquad$

Problem 4: $\qquad$

## TOTAL:

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Possibly useful information:

$$
\begin{aligned}
& \varepsilon_{0}=8.85 \times 10^{-12} \mathrm{C}^{2} \mathrm{~N}^{-1} \mathrm{~m}^{-2} \\
& \mathrm{k}=8.99 \times 10^{9} \mathrm{~N} \mathrm{~m}^{2} \mathrm{C}^{-2} \\
& \mathrm{e}=1.602 \times 10^{-19} \mathrm{C}
\end{aligned}
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A very long conducting tube (hollow cylinder) has an inner radius $a$ and outer radius $b$ and carries a charge per unit length of $+\alpha \mathrm{C} / \mathrm{m}$. A line of charge $+\alpha \mathrm{C} / \mathrm{m}$ lies along the axis of the tube. No current is flowing. For all answers state why.
a. What is the magnitude of the electric field at a radius $\mathrm{r}<a$ ? ( 5 pts .)

b. What is the magnitude of the electric field at a radius $\mathrm{a}<\mathrm{r}<\mathrm{b}$ ? (5 pts.)
c. What is the magnitude of the electric field at a radius $\mathrm{r}>\mathrm{b}$ ? ( 5 pts .)
d. The charge on the cylinder is changed to $-\alpha$. What is the magnitude of the electric field at radius $\mathrm{r}<\mathrm{a}$ ? (5 pts.)
e. The charge on the cylinder remains $-\alpha$. What is the magnitude of the electric field at radius $\mathrm{r}>\mathrm{b}$ ? (5 pts.)
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## PROBLEM 2

A metal (conducting) sphere of radius 0.160 m has a charge of $3.20 \times 10^{-8} \mathrm{C}$.
a. What is the magnitude of the electric field on top of the surface of the sphere? (5 pts.)

b. What is the magnitude of the electric potential on top of the surface of the sphere? (5 pts.)


This sphere is now connected by a long thin conducting wire to an initially uncharged second metal sphere of radius 0.0400 m that is many meters away from the first sphere. After electrostatic equilibrium has been reached (for parts $c, d, e$ ):
c. What is the magnitude of the total charge on the second sphere? (5 pts.)
d. What is the magnitude of the electric potential on top of the surface of the second sphere? (5 pts.)

e. What is the magnitude of the electric field on top of the surface of the second sphere? (5 pts.)
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## PROBLEM 3

A parallel plate capacitor has plate area of $2.00 \times 10^{-1} \mathrm{~m}^{2}$ and plate separation of $1.00 \times 10^{-2} \mathrm{~m}$ and is connected to a power supply that charges it to $3,000.0 \mathrm{~V}$. It is then disconnected from the power supply and a sheet of insulating dielectric is inserted that completely fills the space between the plates. The voltage across the plates decreases to $1,000.0 \mathrm{~V}$.
a. What is the charge on the plates before the power supply is disconnected? (3 pts.)


For the situation before the power supply is disconnected and the dielectric is inserted and for the situation after this is done, please calculate:
b. The capacitance ( 6 pts .)

| Before: | After: |
| :--- | :--- |

c. The magnitude of the field inside the capacitor (6 pts.)

| Before: | After: |
| :--- | :--- |

d. The energy stored in the capacitor (6 pts.)

| Before: | After: |
| :--- | :--- |

After the power supply is disconnected and the dielectric is inserted, please calculate:
e. The permittivity of the dielectric and the induced charge on each face of the dielectric (4 pts.)

| $\varepsilon:$ | $\mathrm{Q}_{\mathrm{i}}:$ |
| :--- | :--- |

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PROBLEM 4
A circuit contains 7 capacitors with $\mathrm{C}_{1}=9.00 \mu \mathrm{~F}$ (one of which is labeled " y ") and 2 capacitors with $\mathrm{C}_{2}=6.00 \mu \mathrm{~F}$ (one of which is labeled "x").
a. What is the equivalent capacitance of this circuit between points $a$ and $b$ ? ( 10 pts.)
Section: $\qquad$
b. Compute the charge on capacitor " x " when $\mathrm{V}_{\mathrm{ab}}=900.0 \mathrm{~V}$. ( 5 pts.)
c. Compute the charge on capacitor " y " when $\mathrm{V}_{\mathrm{ab}}=900.0 \mathrm{~V}$. ( 5 pts.)
d. Compute the voltage $\mathrm{V}_{\mathrm{cd}}$ when $\mathrm{V}_{\mathrm{ab}}=900.0 \mathrm{~V}$. ( 5 pts.)

