

Chapter 28

P28.2 (a) $\Delta V_{\text{term}} = IR$

becomes $10.0 \text{ V} = I(5.60 \ \Omega)$

so $I = \boxed{1.79 \text{ A}}$.

(b) $\Delta V_{\text{term}} = \varepsilon - Ir$

becomes $10.0 \text{ V} = \varepsilon - (1.79 \text{ A})(0.200 \ \Omega)$

so $\varepsilon = \boxed{10.4 \text{ V}}$.

P28.6 (a) $R_p = \frac{1}{\left(\frac{1}{7.00 \ \Omega}\right) + \left(\frac{1}{10.0 \ \Omega}\right)} = 4.12 \ \Omega$

$R_s = R_1 + R_2 + R_3 = 4.00 + 4.12 + 9.00 = \boxed{17.1 \ \Omega}$

(b) $\Delta V = IR$

$34.0 \text{ V} = I(17.1 \ \Omega)$

$I = \boxed{1.99 \text{ A}}$ for $4.00 \ \Omega$, $9.00 \ \Omega$ resistors.

Applying $\Delta V = IR$, $(1.99 \text{ A})(4.12 \ \Omega) = 8.18 \text{ V}$

$8.18 \text{ V} = I(7.00 \ \Omega)$

so $I = \boxed{1.17 \text{ A}}$ for $7.00 \ \Omega$ resistor

$8.18 \text{ V} = I(10.0 \ \Omega)$

so $I = \boxed{0.818 \text{ A}}$ for $10.0 \ \Omega$ resistor.

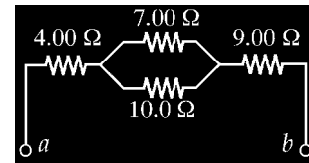


FIG. P28.6

P28.14 When S is open, R_1 , R_2 , R_3 are in series with the battery. Thus:

$$R_1 + R_2 + R_3 = \frac{6 \text{ V}}{10^{-3} \text{ A}} = 6 \text{ k}\Omega. \quad (1)$$

When S is closed in position 1, the parallel combination of the two R_2 's is in series with R_1 , R_3 , and the battery. Thus:

$$R_1 + \frac{1}{2}R_2 + R_3 = \frac{6 \text{ V}}{1.2 \times 10^{-3} \text{ A}} = 5 \text{ k}\Omega. \quad (2)$$

When S is closed in position 2, R_1 and R_2 are in series with the battery. R_3 is shorted. Thus:

$$R_1 + R_2 = \frac{6 \text{ V}}{2 \times 10^{-3} \text{ A}} = 3 \text{ k}\Omega. \quad (3)$$

From (1) and (3): $R_3 = 3 \text{ k}\Omega$.

Subtract (2) from (1): $R_2 = 2 \text{ k}\Omega$.

From (3): $R_1 = 1 \text{ k}\Omega$.

Answers: $\boxed{R_1 = 1.00 \text{ k}\Omega, R_2 = 2.00 \text{ k}\Omega, R_3 = 3.00 \text{ k}\Omega}$.

P28.20 $+15.0 - (7.00)I_1 - (2.00)(5.00) = 0$

$5.00 = 7.00I_1$ so $I_1 = 0.714 \text{ A}$

$I_3 = I_1 + I_2 = 2.00 \text{ A}$

$0.714 + I_2 = 2.00$ so $I_2 = 1.29 \text{ A}$

$+\varepsilon - 2.00(1.29) - 5.00(2.00) = 0$ $\varepsilon = 12.6 \text{ V}$

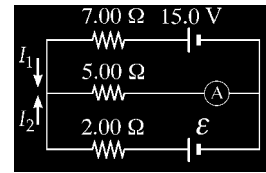


FIG. P28.20

P28.27 Using Kirchoff's rules,

$12.0 - (0.0100)I_1 - (0.0600)I_3 = 0$

$10.0 + (1.00)I_2 - (0.0600)I_3 = 0$

and $I_1 = I_2 + I_3$

$12.0 - (0.0100)I_2 - (0.0700)I_3 = 0$

$10.0 + (1.00)I_2 - (0.0600)I_3 = 0$

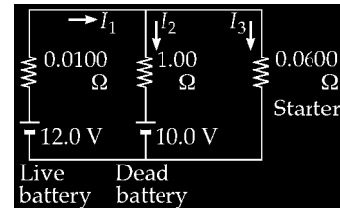


FIG. P28.27

Solving simultaneously,

$I_2 = 0.283 \text{ A downward}$ in the dead battery

and $I_3 = 171 \text{ A downward}$ in the starter.

The currents are forward in the live battery and in the starter, relative to normal starting operation. The current is backward in the dead battery, tending to charge it up.

P28.32 (a) $I(t) = -I_0 e^{-t/RC}$

$I_0 = \frac{Q}{RC} = \frac{5.10 \times 10^{-6} \text{ C}}{(1300 \Omega)(2.00 \times 10^{-9} \text{ F})} = 1.96 \text{ A}$

$I(t) = -(1.96 \text{ A}) \exp\left[\frac{-9.00 \times 10^{-6} \text{ s}}{(1300 \Omega)(2.00 \times 10^{-9} \text{ F})}\right] = -61.6 \text{ mA}$

(b) $q(t) = Q e^{-t/RC} = (5.10 \mu\text{C}) \exp\left[\frac{-8.00 \times 10^{-6} \text{ s}}{(1300 \Omega)(2.00 \times 10^{-9} \text{ F})}\right] = 0.235 \mu\text{C}$

(c) The magnitude of the maximum current is $I_0 = 1.96 \text{ A}$.

P28.36 (a) $\tau = RC = (1.50 \times 10^5 \Omega)(10.0 \times 10^{-6} \text{ F}) = 1.50 \text{ s}$

(b) $\tau = (1.00 \times 10^5 \Omega)(10.0 \times 10^{-6} \text{ F}) = 1.00 \text{ s}$

(c) The battery carries current

$\frac{10.0 \text{ V}}{50.0 \times 10^3 \Omega} = 200 \mu\text{A}$.

The $100 \text{ k}\Omega$ carries current of magnitude

$I = I_0 e^{-t/RC} = \left(\frac{10.0 \text{ V}}{100 \times 10^3 \Omega}\right) e^{-t/1.00 \text{ s}}$.

So the switch carries downward current

$$200 \mu\text{A} + (100 \mu\text{A})e^{-t/1.00 \text{ s}}$$

P28.42 Applying Kirchhoff's loop rule, $-I_g(75.0 \Omega) + (I - I_g)R_p = 0$.

Therefore, if $I = 1.00 \text{ A}$ when $I_g = 1.50 \text{ mA}$,

$$R_p = \frac{I_g(75.0 \Omega)}{(I - I_g)} = \frac{(1.50 \times 10^{-3} \text{ A})(75.0 \Omega)}{1.00 \text{ A} - 1.50 \times 10^{-3} \text{ A}} = \boxed{0.113 \Omega}.$$

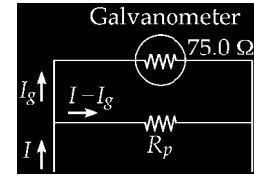


FIG. P28.42

P28.50 $I_{\text{Al}}^2 R_{\text{Al}} = I_{\text{Cu}}^2 R_{\text{Cu}}$ so $I_{\text{Al}} = \sqrt{\frac{R_{\text{Cu}}}{R_{\text{Al}}}} I_{\text{Cu}} = \sqrt{\frac{\rho_{\text{Cu}}}{\rho_{\text{Al}}}} I_{\text{Cu}} = \sqrt{\frac{1.70}{2.82}} (20.0) = 0.776(20.0) = \boxed{15.5 \text{ A}}$

P28.64 The battery supplies energy at a changing rate

Then the total energy put out by the battery is

$$\int dE = \int_{t=0}^{\infty} \frac{\epsilon^2}{R} \exp\left(-\frac{t}{RC}\right) dt$$

$$\int dE = \frac{\epsilon^2}{R} (-RC) \int_0^{\infty} \exp\left(-\frac{t}{RC}\right) \left(-\frac{dt}{RC}\right) = -\epsilon^2 C \exp\left(-\frac{t}{RC}\right) \Big|_0^{\infty} = -\epsilon^2 C [0 - 1] = \epsilon^2 C.$$

The power delivered to the resistor is

So the total internal energy appearing in the resistor is

$$\int dE = \int_0^{\infty} \frac{\epsilon^2}{R} \exp\left(-\frac{2t}{RC}\right) dt$$

$$\int dE = \frac{\epsilon^2}{R} \left(-\frac{RC}{2}\right) \int_0^{\infty} \exp\left(-\frac{2t}{RC}\right) \left(-\frac{2dt}{RC}\right) = -\frac{\epsilon^2 C}{2} \exp\left(-\frac{2t}{RC}\right) \Big|_0^{\infty} = -\frac{\epsilon^2 C}{2} [0 - 1] = \frac{\epsilon^2 C}{2}.$$

The energy finally stored in the capacitor is $U = \frac{1}{2} C(\Delta V)^2 = \frac{1}{2} C\epsilon^2$. Thus, energy of the circuit is conserved

$\epsilon^2 C = \frac{1}{2} \epsilon^2 C + \frac{1}{2} \epsilon^2 C$ and resistor and capacitor share equally in the energy from the battery.