

Chapter 32

P32.4 $L = \frac{N\Phi_B}{I} \rightarrow \Phi_B = \frac{LI}{N} = \boxed{240 \text{ nT} \cdot \text{m}^2}$ through each turn

P32.6 From $\mathcal{E} = L \left(\frac{\Delta I}{\Delta t} \right)$, we have $L = \frac{\mathcal{E}}{(\Delta I/\Delta t)} = \frac{24.0 \times 10^{-3} \text{ V}}{10.0 \text{ A/s}} = 2.40 \times 10^{-3} \text{ H}$.

From $L = \frac{N\Phi_B}{I}$, we have $\Phi_B = \frac{LI}{N} = \frac{(2.40 \times 10^{-3} \text{ H})(4.00 \text{ A})}{500} = \boxed{19.2 \mu\text{T} \cdot \text{m}^2}$.

P32.22 $I = I_{\text{max}}(1 - e^{-t/\tau})$: $0.980 = 1 - e^{-3.00 \times 10^{-3} t}$

$$0.020 = e^{-3.00 \times 10^{-3} t}$$

$$\tau = -\frac{3.00 \times 10^{-3}}{\ln(0.020)} = 7.67 \times 10^{-4} \text{ s}$$

$$\tau = \frac{L}{R}, \text{ so } L = \tau R = (7.67 \times 10^{-4})(10.0) = \boxed{7.67 \text{ mH}}$$

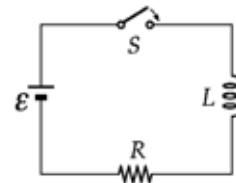


FIG. P32.22

P32.36

From Equation 32.7, $I = \frac{\mathcal{E}}{R}(1 - e^{-Rt/L})$.

(a) The maximum current, after a long time t , is $I = \frac{\mathcal{E}}{R} = 2.00 \text{ A}$.

At that time, the inductor is fully energized and

(b)

(c)

(d) $U = \frac{LI^2}{2} = \frac{(10.0 \text{ H})(2.00 \text{ A})^2}{2} = \boxed{20.0 \text{ J}}$

P32.38 The total magnetic energy is the volume integral of the energy density, $u = \frac{B^2}{2\mu_0}$.

Because B changes with position, u is not constant. For $B = B_0 \left(\frac{R}{r} \right)^2$, $u = \left(\frac{B_0^2}{2\mu_0} \right) \left(\frac{R}{r} \right)^4$.

Next, we set up an expression for the magnetic energy in a spherical shell of radius r and thickness dr . Such a shell has a volume $4\pi r^2 dr$, so the energy stored in it is

$$dU = u(4\pi r^2 dr) = \left(\frac{2\pi B_0^2 R^4}{\mu_0} \right) \frac{dr}{r^2}.$$

We integrate this expression for $r = R$ to $r = \infty$ to obtain the total magnetic energy outside the sphere. This gives

$$U = \frac{2\pi B_0^2 R^3}{\mu_0} = \frac{2\pi(5.00 \times 10^{-5} \text{ T})^2(6.00 \times 10^6 \text{ m})^3}{(1.26 \times 10^{-6} \text{ T} \cdot \text{m/A})} = \boxed{2.70 \times 10^{18} \text{ J}}.$$

P32.39 $I_1(t) = I_{\max} e^{-\alpha t} \sin \omega t$ with $I_{\max} = 5.00 \text{ A}$, $\alpha = 0.025 \text{ s}^{-1}$, and $\omega = 377 \text{ rad/s}$

$$\frac{dI_1}{dt} = I_{\max} e^{-\alpha t} (-\alpha \sin \omega t + \omega \cos \omega t).$$

At $t = 0.800 \text{ s}$,

$$\frac{dI_1}{dt} = (5.00 \text{ A/s}) e^{-0.0200} \left[-(0.025 \text{ s}^{-1}) \sin(0.800(377)) + 377 \cos(0.800(377)) \right]$$

$$\frac{dI_1}{dt} = 1.85 \times 10^3 \text{ A/s}.$$

$$\text{Thus, } \varepsilon_2 = -M \frac{dI_1}{dt}: \quad M = \frac{-\varepsilon_2}{dI_1/dt} = \frac{+3.20 \text{ V}}{1.85 \times 10^3 \text{ A/s}} = \boxed{1.73 \text{ mH}}.$$

P32.51 (a) $f = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(0.082 \text{ H})(17.0 \times 10^{-6} \text{ F})}} = \boxed{135 \text{ Hz}}$

(b) $Q = Q_{\max} \cos \omega t = (180 \text{ } \mu\text{C}) \cos(847 \times 0.001 \text{ s}) = \boxed{119 \text{ } \mu\text{C}}$

(c) $I = \frac{dQ}{dt} = -\omega Q_{\max} \sin \omega t = -(847)(180) \sin(0.847) = \boxed{-114 \text{ mA}}$

P32.54 (a) $\omega_d = \sqrt{\frac{1}{LC} - \left(\frac{R}{2L}\right)^2} = \sqrt{\frac{1}{(2.20 \times 10^{-3})(1.80 \times 10^{-6})} - \left(\frac{7.60}{2(2.20 \times 10^{-3})}\right)^2} = 1.58 \times 10^4 \text{ rad/s}$

Therefore, $f_d = \frac{\omega_d}{2\pi} = \boxed{2.51 \text{ kHz}}$.

(b) $R_c = \sqrt{\frac{4L}{C}} = \boxed{69.9 \text{ } \Omega}$