

HOMEWORK 2

Physics 751
Advanced Solid State Physics
Fall, 2001

1. Show that the damping of long-lived single particle excitations is given by

$$\gamma(p) = \text{Im}\Sigma(\epsilon(p), p) * \left[1 - \frac{\partial \text{Re}\Sigma(\omega, p)}{\partial \omega} \Big|_{\omega=\epsilon(p)}\right]^{-1} \quad (1)$$

2. Polarization operator is defined as

$$\Pi(k, \omega) = \int \frac{d^3q d\Omega}{(2\pi)^4} G(q, \Omega) G(k + q, \omega + \Omega) \quad (2)$$

Compute $\Pi(k, 0)$ for a free Fermi gas and analyze the behavior of $\Pi(k, 0)$ at $|k| \approx k_F$.

3. Show that in a degenerate electron gas

$$\Sigma(q, \omega) = -\frac{e^2}{2\pi} \left(\frac{p_F^2 - q^2}{q} \log \left| \frac{p_F + q}{p_F - q} \right| + 2p_F \right) \quad (3)$$

Sketch the resulting single-particle spectrum and compare the effective mass with the result that we obtained before.