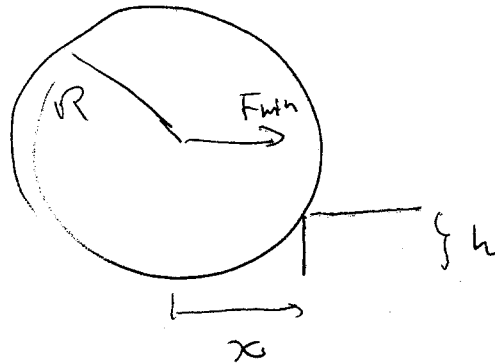


Example: Raising a wheel

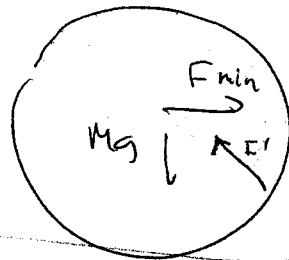
(Push a cart up the stairs)



What is  $F_{min}$  necessary to raise the wheel over the step?

$F_n = 0$

Free body diagram



$F$  direction & magnitude are unknown

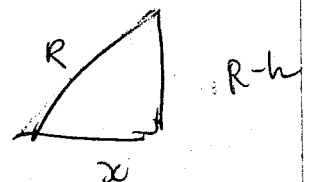
$\Rightarrow$  Choose pt of contact as O

$$F_{min}(R-h) - Mg x = 0$$

$$F_{min} = \frac{Mg x}{R-h}$$

Express  $x$  in terms of  $h$

$$x^2 + (R-h)^2 = R^2$$



$$x = \sqrt{2Rh - h^2} = \sqrt{h(2R-h)}$$

Hence

$$F_{\min} = \frac{Mg \sqrt{h(2R-h)}}{R-h}$$

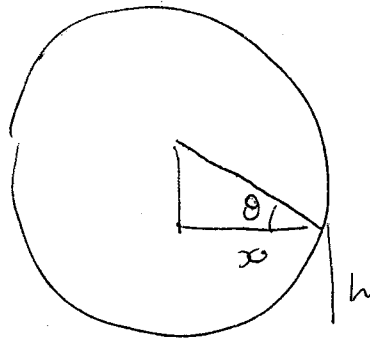
check (2)

$$\left\{ \begin{array}{l} h \rightarrow R \quad F_{\min} \rightarrow \infty \\ h \rightarrow 0 \quad F_{\min} \rightarrow 0 \end{array} \right.$$

We have chosen O as pivot point to get rid of  $\vec{F}'$  in eqn.

Direction of  $\vec{F}'$ ? Choose O as center of wheel  
 $\Rightarrow \vec{F}'$  must pt towards the center  
otherwise there is a torque

Magnitude of  $\vec{F}'$ ?  $\sum \vec{F} = 0$



$$F' \cos \theta = F_{\min}$$

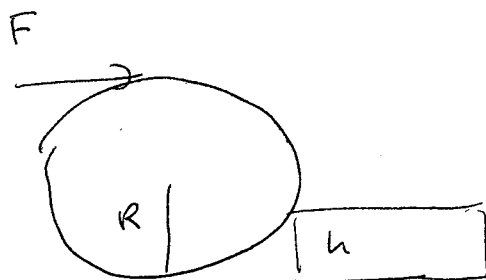
$$F' \sin \theta = Mg$$

$$F' = \sqrt{F_{\min}^2 + (Mg)^2}$$

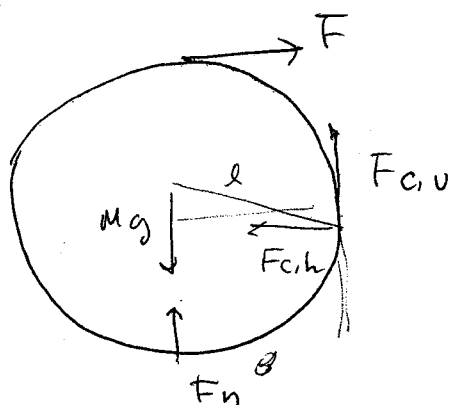
#

A slightly different example

(Ch 12 # 35)



Free body diagram



Torque about contact pt (why?).

$$Mg\ell - F_n\ell - F(2R-h) = 0$$

$$F_n = Mg - \frac{F(2R-h)}{\ell}$$

Express  $\ell$  in terms of  $R$  &  $h$

$$\ell = \sqrt{R(2R-h)}$$

$$F_n = Mg - \frac{F(2R-h)}{\sqrt{h(2R-h)}}$$

In partaller  $F_n = 0$  wheel off the ground

when  $F_{min} = \frac{Mg \sqrt{h(2R-h)}}{2R-h}$   
 ↑  
 only difference

check  $F_{min} = \begin{cases} 0 & \text{as } h \rightarrow 0 \\ \infty & \text{as } h = 2R \end{cases}$

$\vec{F}_c$  at contact pt is no longer pointing towards the center of wheel. Why? (ext  $\vec{F}$  provides a torque)

Newton's laws  $F_{c,h} = F$

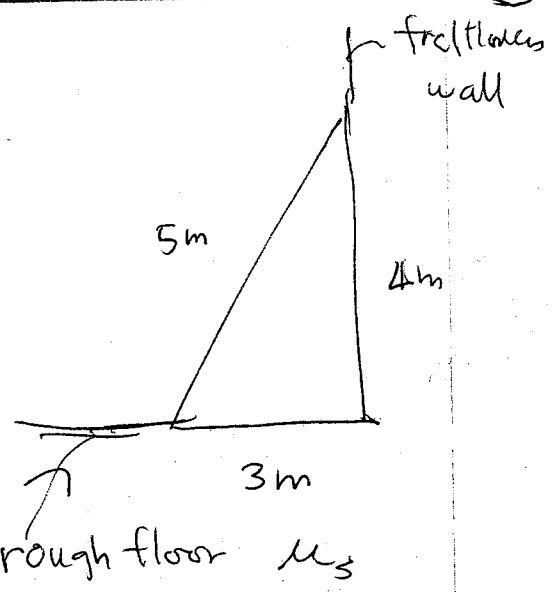
$$F_{c,v} = Mg - F_n$$

$$= \frac{F(2R-h)}{\sqrt{h(2R-h)}}$$

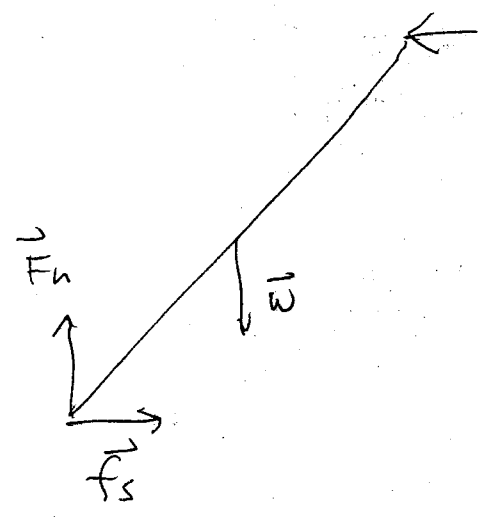
↳ can find the angle of  $\vec{F}_c$

# Example Leaning Ladder

What is min  $\mu_s$  for ladder not to slip?



## Free body diagram



$F_1$  why this direction?

Newton's law: =  $f_s = F_1$   
 $F_n = W$

to find  $\mu_s$  Need to find  $f_s$  in terms of  $F_n$ .

First find  $F_1$  in terms of  $W$ .

Choose 0 to be foot of ladder

$$\sum \vec{C} = 0 \Rightarrow F_1(4m) - W(1.5m) = 0$$

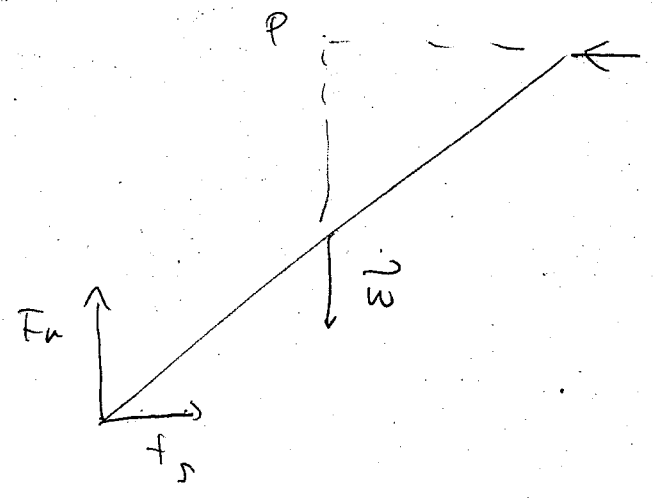
$$F_1 = \frac{3}{8} W$$

Since  $f_s \leq \mu_s F_n$  no slipping

$$\mu_{s, \min} = \frac{f_s}{F_n}$$

$$\Rightarrow \mu_{s, \min} = \frac{F_1}{W} = \frac{3}{8}$$

Alternatively, choose another pt P as pivot pt



No torque due to  $\vec{F}_1$  &  $\vec{W}$  at P

$$\Rightarrow F_n (1.5\text{m}) = f_s (4\text{m})$$

$$\Rightarrow \mu_{s, \min} = \frac{F_s}{F_n} = \frac{3}{8} \quad \checkmark$$