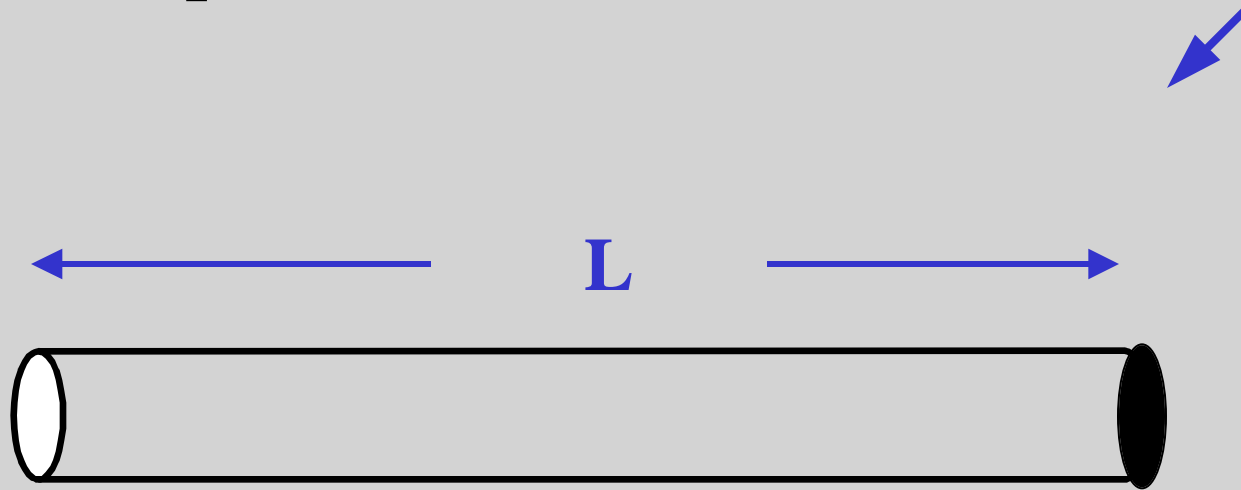


Closed Pipe

Pipe closed at ONE end:



$$\leftarrow L = \frac{\lambda}{4} \rightarrow$$

fundamental frequency of closed pipe:

$$f_1 = \frac{v}{4L}$$

note: this is half the frequency of an open pipe of same length (octave below)

open end: pressure **NODE (motion antinode)
closed end: pressure **antinode** (motion node)**

example:

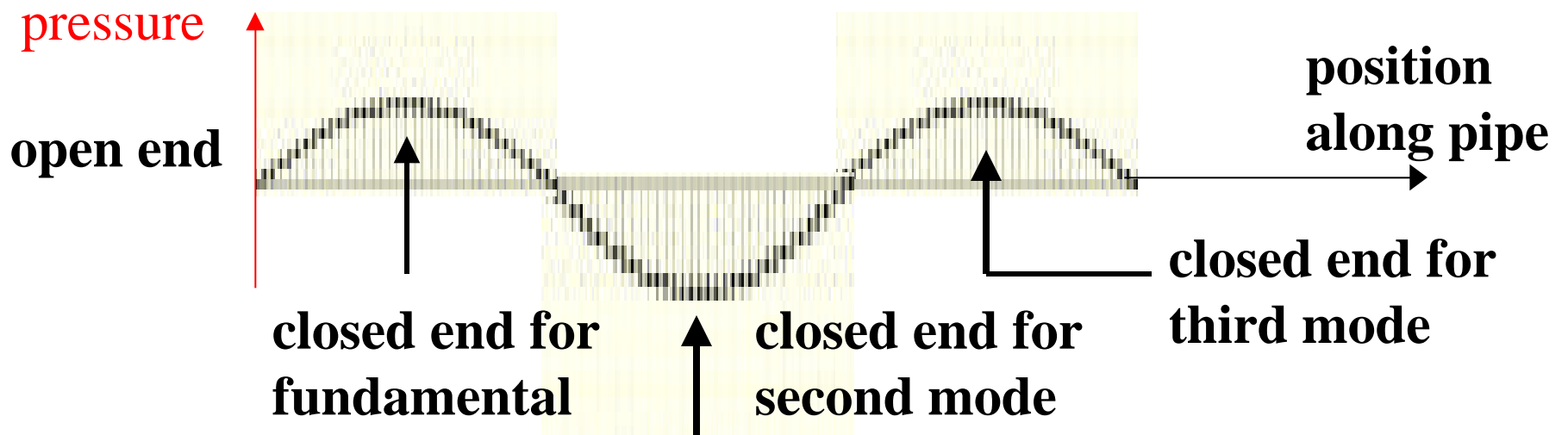
how long is a **CLOSED** organ pipe that plays $A_1 = 55 \text{ Hz}$? (note: $A_1 \rightarrow A_4 = 3$ octaves)

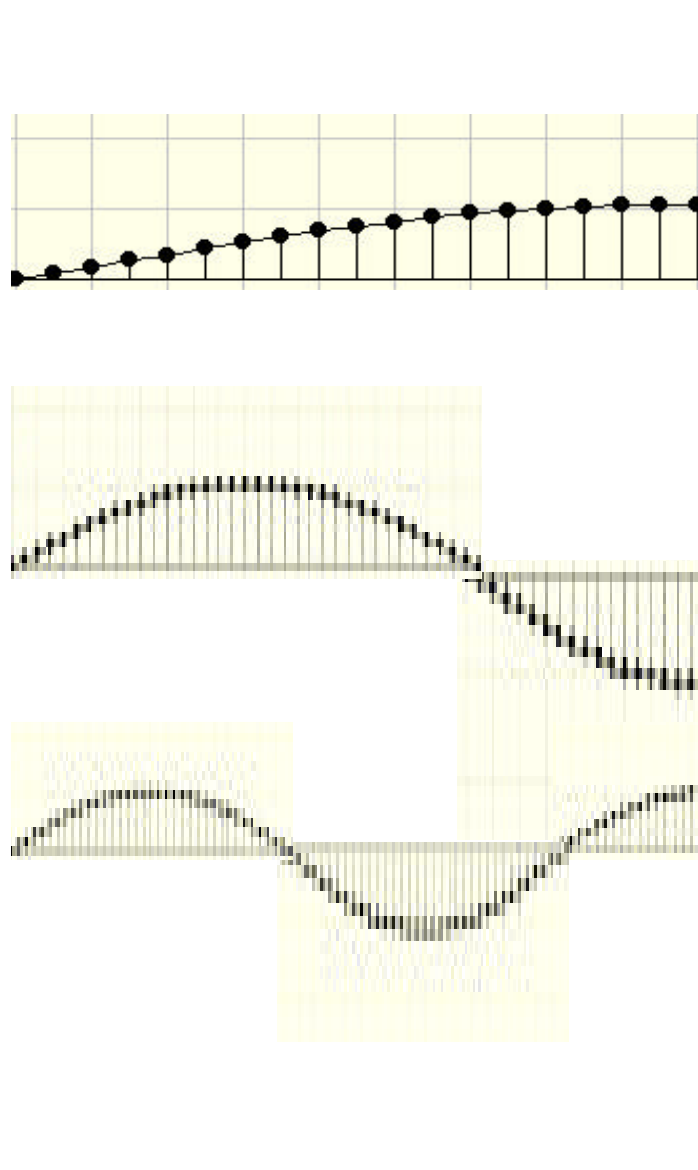
$$L = v/4f = (340/220) \text{ m} = \underline{1.55} = \underline{5 \text{ ft}}$$

Higher modes of closed pipe:

need pressure NODE at open end

need pressure BELLY at closed end





higher modes (overtones) of closed pipe

Only ODD multiples of fundamental

f_1 first mode (fundamental)

$3f_1$ second mode (first overtone)

but third harmonic!

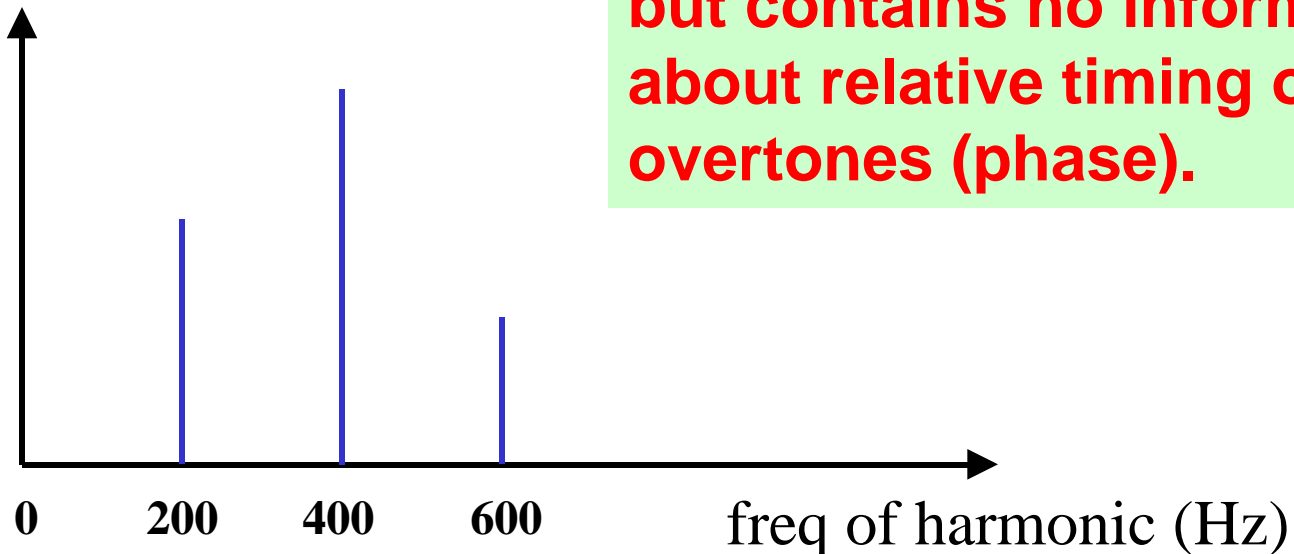
$5f_1$ third mode (second overtone)

but fifth harmonic!

Sound Spectrum (Fourier Spectrum)

Fourier: represent complicated **periodic** oscillation (period T) as sum of sinusoidal oscillations of frequencies $f_1 = (1/T)$ and harmonics $f_2 = 2f_1$, $f_3 = 3f_1$ etc.

amplitude
of harmonic



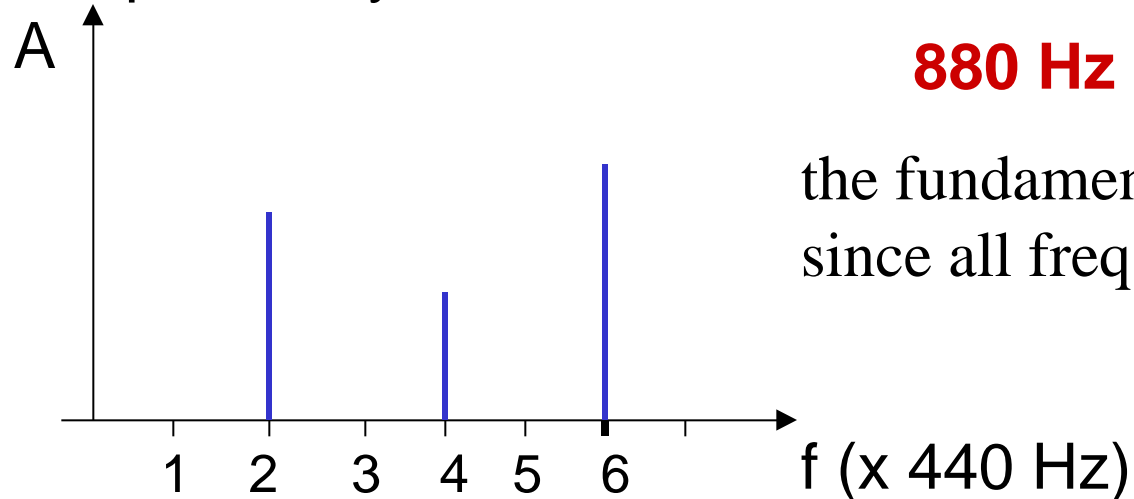
easy visualization of harmonic content (timbre) but contains no information about relative timing of overtones (phase).

Fourier Synthesizer..... produces frequencies
 $f_1, 2f_1, 3f_1, 4f_1, 5f_1, 6f_1, 7f_1$ etc
of adjustable amplitude and phase .

**e.g. $f_1 = 440 \text{ Hz} = A_4$ can synthesize any
oscillation of period $T=1/440$ sec.**

Pitch perception

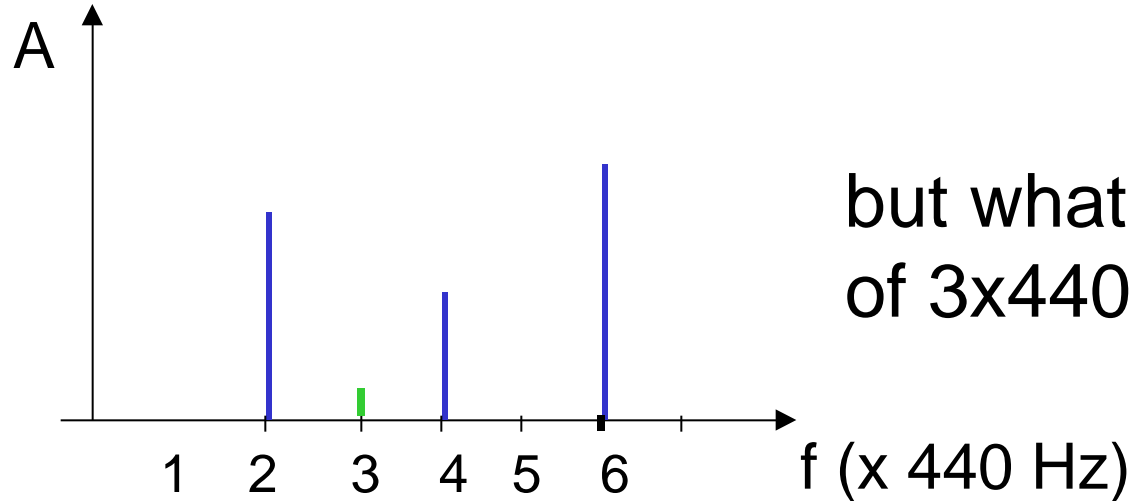
listen to the following combination of harmonics:
what pitch do you hear?



880 Hz = A_5

the fundamental is 880 Hz
since all freq multiples of 880

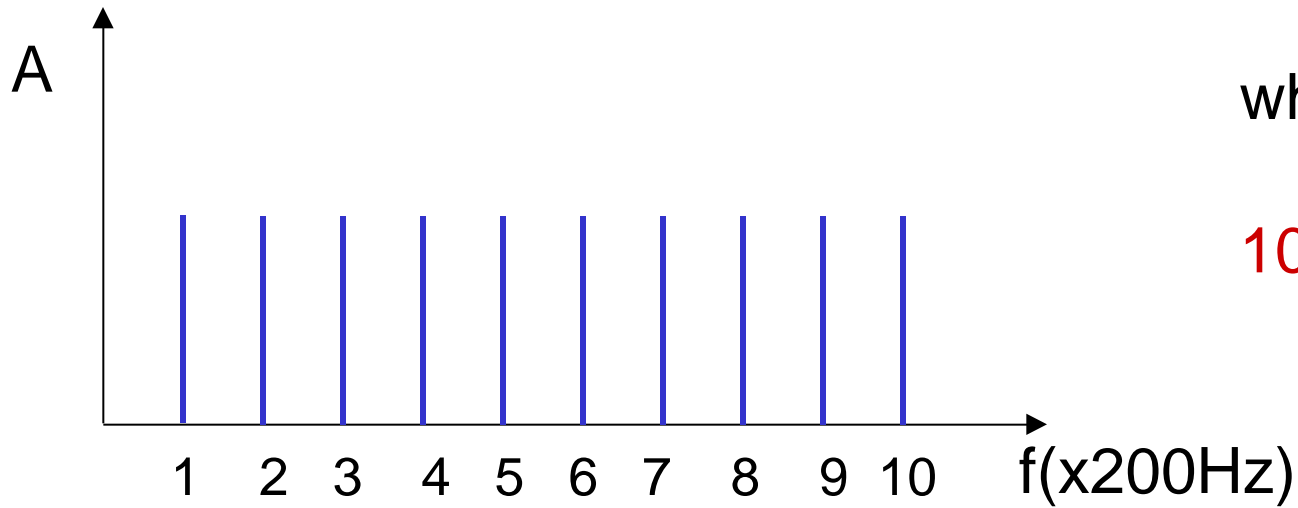
but....



but what if we add a **bit**
of $3 \times 440 \text{ Hz}$??

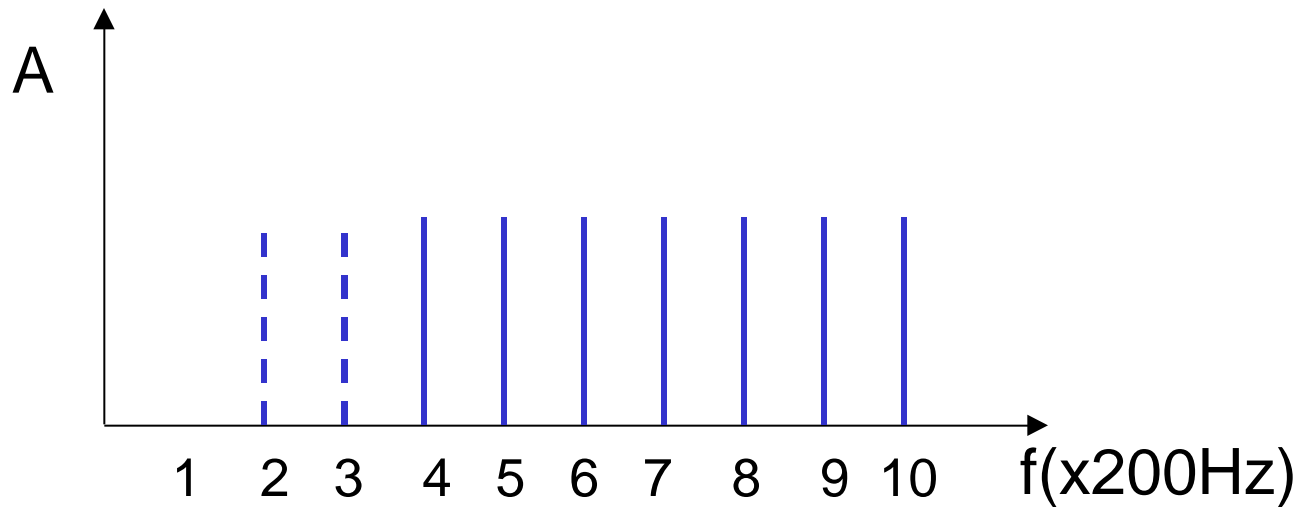
now suddenly the (theoretical) fundamental is 440 Hz
but what do we hear?

Demo: in some situations (missing or almost missing
fundamental) there may be an ambiguity in perceived pitch



what do you hear?

100 Hz of course!



and now?

DEMO



Tone Quality (Timbre)

In acoustic theory, what exactly is “timbre”?
Timbre is that attribute that differentiates two tones of same loudness and same pitch.

The Fourier Spectrum (frequencies and intensities of overtones) is only one aspect of timbre.....

Other aspect of tone quality: rise and decay

An example of two tonal presentations which show importance of the tone envelope (attack and decay)

