

P5.34 (a) Pulley P_1 has acceleration a_2 .
 Since m_1 moves *twice* the distance P_1 moves in the same time, m_1 has twice the acceleration of P_1 , i.e., $a_1 = 2a_2$.

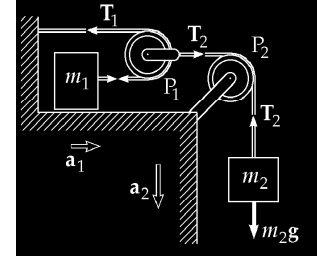


FIG. P5.34

(b) From the figure, and using

$$\begin{aligned} \sum F = ma: \quad m_2g - T_2 &= m_2a_2 & (1) \\ T_1 &= m_1a_1 = 2m_1a_2 & (2) \\ T_2 - 2T_1 &= 0 & (3) \end{aligned}$$

Equation (1) becomes $m_2g - 2T_1 = m_2a_2$. This equation combined with Equation (2) yields

$$\frac{T_1}{m_1} \left(2m_1 + \frac{m_2}{2} \right) = m_2g$$

$$\boxed{T_1 = \frac{m_1m_2}{2m_1 + \frac{1}{2}m_2} g} \quad \text{and} \quad \boxed{T_2 = \frac{m_1m_2}{m_1 + \frac{1}{4}m_2} g}$$

(c) From the values of T_1 and T_2 we find that

$$a_1 = \frac{T_1}{m_1} = \frac{m_2g}{2m_1 + \frac{1}{2}m_2} \quad \text{and} \quad a_2 = \frac{1}{2}a_1 = \frac{m_2g}{4m_1 + m_2}$$

P5.37 $\sum F_y = ma_y: \quad +n - mg = 0$
 $f_s \leq \mu_s n = \mu_s mg$

This maximum magnitude of static friction acts so long as the tires roll without skidding.

$$\sum F_x = ma_x: \quad -f_s = ma$$

The maximum acceleration is

$$a = -\mu_s g.$$

The initial and final conditions are: $x_i = 0$, $v_i = 50.0 \text{ mi/h} = 22.4 \text{ m/s}$, $v_f = 0$

$$v_f^2 = v_i^2 + 2a(x_f - x_i): \quad -v_i^2 = -2\mu_s g x_f$$

(a) $x_f = \frac{v_i^2}{2\mu_s g}$
 $x_f = \frac{(22.4 \text{ m/s})^2}{2(0.100)(9.80 \text{ m/s}^2)} = \boxed{256 \text{ m}}$

(b) $x_f = \frac{v_i^2}{2\mu_s g}$
 $x_f = \frac{(22.4 \text{ m/s})^2}{2(0.600)(9.80 \text{ m/s}^2)} = \boxed{42.7 \text{ m}}$

P5.44 Let a represent the positive magnitude of the acceleration $-\hat{a}\mathbf{j}$ of m_1 , of the acceleration $-\hat{a}\mathbf{i}$ of m_2 , and of the acceleration $+\hat{a}\mathbf{j}$ of m_3 . Call T_{12} the tension in the left rope and T_{23} the tension in the cord on the right.

$$\text{For } m_1, \quad \sum F_y = ma_y \quad +T_{12} - m_1g = -m_1a$$

$$\text{For } m_2, \quad \sum F_x = ma_x \\ -T_{12} + \mu_k n + T_{23} = -m_2a$$

$$\text{and} \quad \sum F_y = ma_y \quad n - m_2g = 0$$

$$\text{for } m_3, \quad \sum F_y = ma_y \quad T_{23} - m_3g = +m_3a$$

we have three simultaneous equations

$$\begin{aligned} -T_{12} + 39.2 \text{ N} &= (4.00 \text{ kg})a \\ +T_{12} - 0.350(9.80 \text{ N}) - T_{23} &= (1.00 \text{ kg})a \\ +T_{23} - 19.6 \text{ N} &= (2.00 \text{ kg})a. \end{aligned}$$

(a) Add them up:

$$+39.2 \text{ N} - 3.43 \text{ N} - 19.6 \text{ N} = (7.00 \text{ kg})a$$

$$a = \boxed{2.31 \text{ m/s}^2}, \text{ down for } m_1, \text{ left for } m_2, \text{ and up for } m_3.$$

(b) Now $-T_{12} + 39.2 \text{ N} = (4.00 \text{ kg})(2.31 \text{ m/s}^2)$

$$\boxed{T_{12} = 30.0 \text{ N}}$$

$$\text{and } T_{23} - 19.6 \text{ N} = (2.00 \text{ kg})(2.31 \text{ m/s}^2)$$

$$\boxed{T_{23} = 24.2 \text{ N}}.$$

P5.54

$$18 \text{ N} - P = (2 \text{ kg})a$$

$$P - Q = (3 \text{ kg})a$$

$$Q = (4 \text{ kg})a$$

Adding gives $18 \text{ N} = (9 \text{ kg})a$ so

$$a = \boxed{2.00 \text{ m/s}^2}.$$

$$(b) \quad Q = 4 \text{ kg}(2 \text{ m/s}^2) = \boxed{8.00 \text{ N net force on the 4 kg}}$$

$$P - 8 \text{ N} = 3 \text{ kg}(2 \text{ m/s}^2) = \boxed{6.00 \text{ N net force on the 3 kg}} \text{ and } P = 14 \text{ N}$$

$$18 \text{ N} - 14 \text{ N} = 2 \text{ kg}(2 \text{ m/s}^2) = \boxed{4.00 \text{ N net force on the 2 kg}}$$

$$(c) \quad \text{From above, } Q = \boxed{8.00 \text{ N}} \text{ and } P = \boxed{14.0 \text{ N}}.$$

(d) The 3-kg block models the heavy block of wood. The contact force on your back is represented by Q , which is much less than the force F . The difference between F and Q is the net force causing

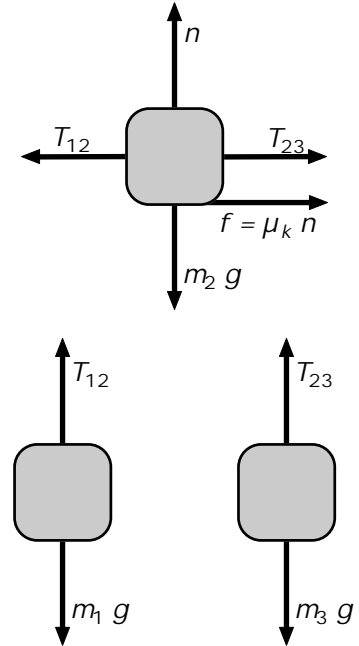


FIG. P5.44

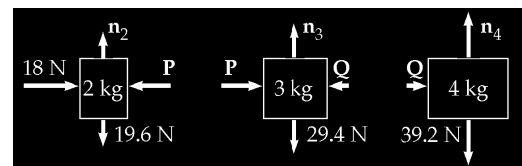


FIG. P5.54

acceleration of the 5-kg pair of objects. The acceleration is real and nonzero, but lasts for so short a time that it never is associated with a large velocity. The frame of the building and your legs exert forces, small relative to the hammer blow, to bring the partition, block, and you to rest again over a time large relative to the hammer blow. This problem lends itself to interesting lecture demonstrations. One person can hold a lead brick in one hand while another hits the brick with a hammer.

P5.68 Since it has a larger mass, we expect the 8.00-kg block to move down the plane. The acceleration for both blocks should have the same magnitude since they are joined together by a non-stretching string. Define up the left hand plane as positive for the 3.50-kg object and down the right hand plane as positive for the 8.00-kg object.

$$\begin{aligned} \sum F_1 = m_1 a_1: & \quad -m_1 g \sin 35.0^\circ + T = m_1 a \\ \sum F_2 = m_2 a_2: & \quad m_2 g \sin 35.0^\circ - T = m_2 a \end{aligned}$$

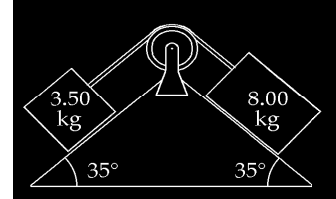


FIG. P5.68

and

$$\begin{aligned} -(3.50)(9.80) \sin 35.0^\circ + T &= 3.50a \\ (8.00)(9.80) \sin 35.0^\circ - T &= 8.00a. \end{aligned}$$

Adding, we obtain

$$+45.0 \text{ N} - 19.7 \text{ N} = (11.5 \text{ kg})a.$$

(b) Thus the acceleration is

$$a = 2.20 \text{ m/s}^2.$$

By substitution,

$$-19.7 \text{ N} + T = (3.50 \text{ kg})(2.20 \text{ m/s}^2) = 7.70 \text{ N}.$$

(a) The tension is

$$T = 27.4 \text{ N}.$$