

Phys 201
no office hour today (11/30)

last time: heat ΔQ
heat added depends
on process.

transfer variables: depends on process ΔQ

state variables: volume V
pressure P
temperature T } do not depend
on procedure

§ 20.4 Work
transfer variable



work done by piston
on gas when piston
moves by $-dx \hat{i}$

$$\begin{aligned} dW &= \vec{F} \cdot d\vec{r} \\ &= -F_x dx \\ &= -P A dx \\ &= -P dV \end{aligned}$$

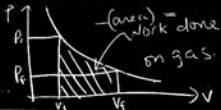
pressure volume change

$$dw = -PdV$$

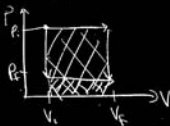
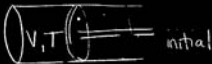
if change V by a lot,

$$W = -\int_{V_i}^{V_f} P(V) dV$$

if you know $P(V)$, then
can calculate work



Work is transfer variable



path 1
pull piston out slowly
piston does negative work
on gas

path 2
punch hole in piston
piston does no work
on gas

How to describe relationship
between state variables and
transfer variables

- laws of thermodynamics

1st law of thermodynamics

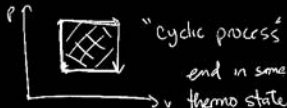
$$\Delta E_{int} = Q + W$$

\uparrow internal energy \uparrow heat added \curvearrowright work done on system

Q, W transfer variables but Q+W is state variable

for infinitesimal changes of stat,

$$dE_{int} = dQ + dW$$



E_{int} is state variable

$$\Rightarrow \text{for cyclic process } \Delta Q = -\Delta W$$

§20.6 Examples of 1st law

$$[dE_{int} = dQ + dW]$$

1) adiabatic process ^{def} ($\Delta Q = 0$)

$$\Delta E_{int} = \underset{\substack{\uparrow \\ \text{Work done on system}}}{W} \left(\int_{V_i}^{V_f} P dV \right)$$

2) isobaric constant pressure
work done $W = -P(V_f - V_i)$

3) Iso volumetric process (constant volume)

$$\Delta W = 0$$

$$\rightarrow \Delta E_{int} = Q$$

4) Isothermal process (constant T)
for ideal gas

calculate work done when expand isothermally.

T fixed

start at V_i end at V_f

for ideal gas.

$$PV = nRT$$

$$P = \frac{nRT}{V}$$

work done on gas

$$W = - \int_{V_i}^{V_f} P dV = - \int_{V_i}^{V_f} \left(\frac{nRT}{V} \right) dV = nRT \int_{V_i}^{V_f} \frac{dV}{V} = nRT \ln \left(\frac{V_f}{V_i} \right)$$

