

NAME: _____, Sect. # _____

Physics 109 Homework # 2
due Monday, September 24, 2001

1. Damping time: a guitar string has a frequency of 260 Hz (middle-C) and a damping time of 2 sec.

a) How many oscillations does the string make before the amplitude has decreased to half of the original value?

$$f = 260 \text{ Hz} = 260 \text{ osc/sec}; \text{ in } 2 \text{ sec: } 2 \times 260 = \underline{520 \text{ oscillations}}$$

b) if the initial amplitude of the guitar string was 2 mm, how large will be the amplitude

after 2 sec? $\underline{1 \text{ mm}}$ after 4 sec? $\underline{\frac{1}{2} \text{ mm}}$ after 8 sec? $\underline{\frac{1}{8} \text{ mm}}$

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 $= 4 \tau \text{ thus } (\frac{1}{2})^4 \times 2 \text{ mm}$

2. In the lecture demo we found that a 2 kg mass oscillating up and down on a spring

made 10 oscillations in 5 sec, which corresponds to a frequency of $\underline{2}$ Hz. ($f = \frac{1}{T} = \frac{1}{0.5 \text{ s}}$)

What would have been the frequency if the 2 kg mass was replaced by a 4 kg mass?

(hint: look at the SHO frequency formula and use proportions like we did in lecture).

$$f = \frac{1}{2\pi} \sqrt{k/m} \quad \text{larger mass} \rightarrow \text{lower } f \quad f = \frac{2 \text{ Hz}}{\sqrt{2}} = \underline{1.4 \text{ Hz}}$$

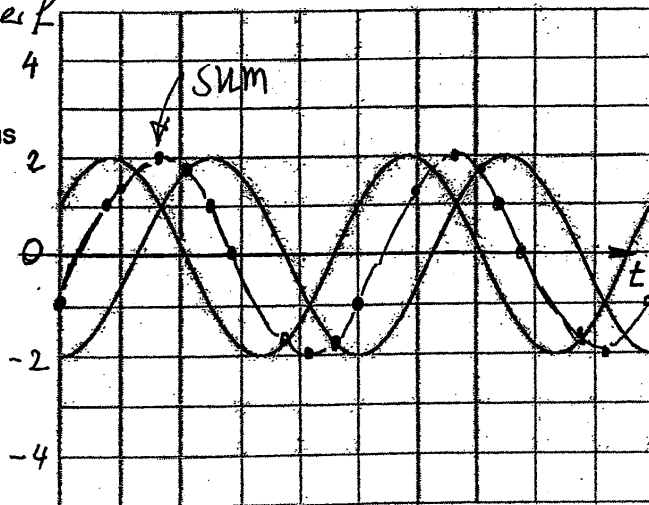
$$2 \times \text{larger mass} \rightarrow \sqrt{2} \times \text{lower } f \quad (m \text{ is under } \sqrt{\quad})$$

What would have been the frequency if the 2 kg mass was replaced by a 1 kg mass?

lower $m \rightarrow$ higher f
 $2 \times \text{lower } m \rightarrow \sqrt{2} \times \text{higher } f$
 $f = 2 \times \sqrt{2} = \underline{2.8 \text{ Hz}}$

3. The graph shows the pressure variations from two separate tuning forks.

Show the superposition of the two oscillations, i.e. the pressure variation when both tuning forks oscillate at the same time.



43. Beats: A tuning fork has a frequency of 440 Hz. What are the possible frequencies of a second tuning fork if, when both forks are sounded together, they produce 4 beats every second?

beat frequency $4\text{ Hz} = \text{freq. difference between the two forks.}$

Thus either 444 Hz or 436 Hz

5. A simple harmonic oscillator has a natural frequency of 200 Hz. The damping time of the oscillator is 40 ms.

A periodic force is applied to the oscillator.

- For what frequency of this force does one observe the largest amplitude of oscillation?

at 200 Hz

- about how many Hz would the frequency have to be raised or lowered to get half as much amplitude of the oscillator?

$$\Delta f \cdot \tau = 4/q \rightarrow \Delta f = \frac{4/q}{40 \times 10^{-3}} = \frac{0.44 \times 1000}{40} = 11 \text{ Hz}$$

raise or lower by $\frac{1}{2} \times 11 \text{ Hz} = 5.5 \text{ Hz}$ (since Δf is full)

- When one plots a resonance curve, the horizontal axis shows what quantity? (width)

The horizontal axis shows freq. of driving (pushing) force

- The vertical axis shows what quantity?

The vertical axis shows amplitude of oscillating system

- Based on the above make an approximate drawing of the resonance curve.

