

NAME: _____, Sect. # _____

Physics 109 **Homework #5** due Monday Oct. 15, 2001

Formulae: in air $v = 340\text{m/s}$. **Open:** $f_1 = v/2L$; $f_n = nf_1$; **Closed:** $f_1 = v/4L$

Exercises on pipes:

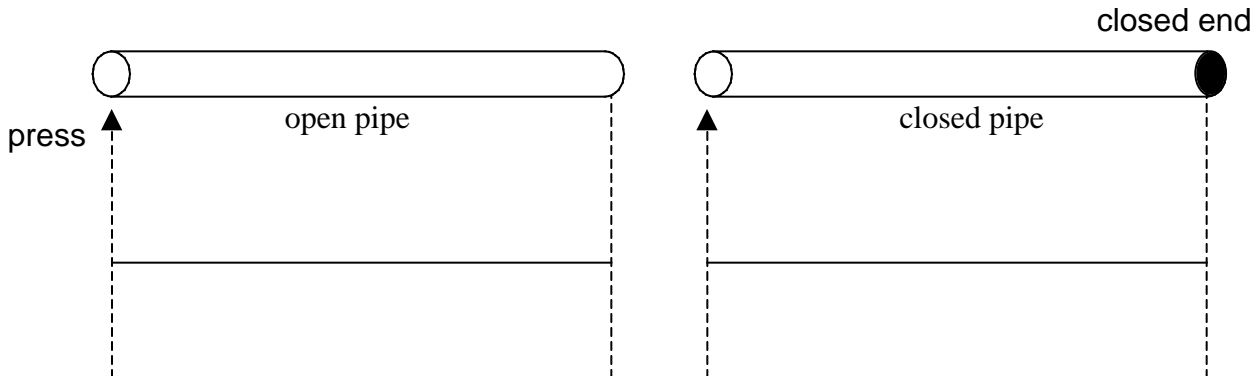
1. (a) Find the fundamental frequency and the frequencies of the first two overtones of an open pipe of **60 cm** length.

_____ Hz, _____ Hz, _____ Hz.

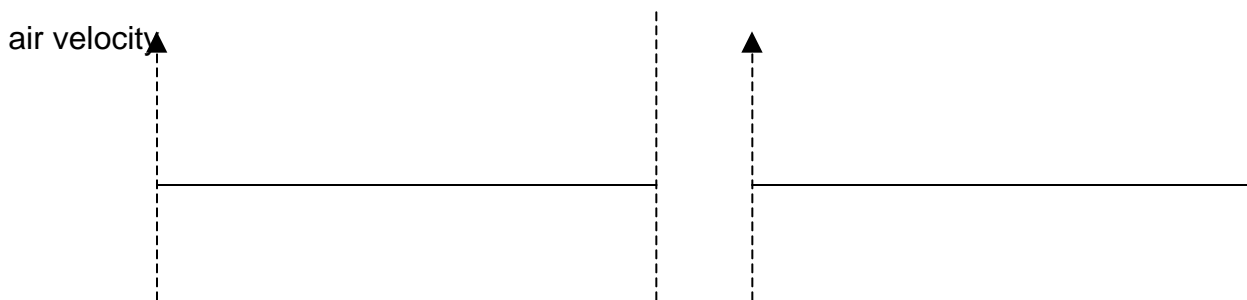
- (b) if the same pipe is closed at one end, what are the corresponding frequencies?

_____ Hz, _____ Hz, _____ Hz.

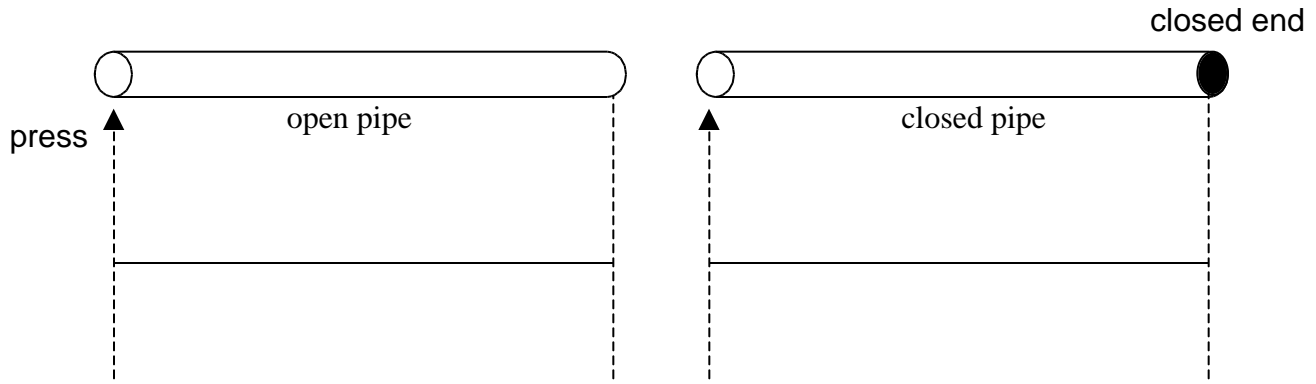
2. (a) Make a graph of the **pressure** at different instances in an open pipe (left) and in a closed pipe (right) oscillating in the fundamental mode.
(hint: first mark the pressure nodes by letter **N** - then draw the curves)



- make a corresponding graph or the air **velocity** distribution in the pipe.
(remember slinky demo - where does it move most, where does it not move at all?)



(b) make corresponding **pressure** graphs for the **next higher mode**.



3. Between room temperature (20°C) and body temperature (37°C) the speed of sound increases by 10 m/s . A flute has a frequency of 260 Hz when it is cold. Find the frequency when the flute is warmed to body temperature by the flutist's breath (hint: use proportions to relate frequencies to speed of sound - what is the ratio of speed of sound at the two temperatures? What is the frequency ratio?)

$$f = \underline{\hspace{2cm}}$$

Exercises on Fourier Analysis

NOTE: we can usually not figure out the amplitudes of the overtones, but can only find out which are present and what their frequencies are. Thus when you are asked to draw a Fourier spectrum the position of the Fourier components should be in the right place, but the intensity is arbitrary.

4 a) What might the Fourier spectrum of a closed pipe with fundamental frequency 300 Hz look like?

(b) What is the spectrum when the same pipe is open at both ends?



5. What might the Fourier spectrum of a 500 Hz violin string look like when it is plucked $1/3$ the length from one end?

